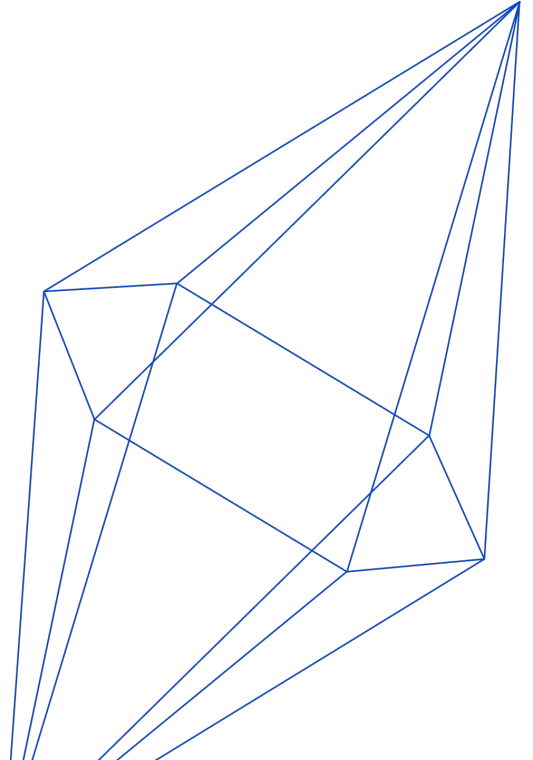




# PHSafe: The Disclosure Avoidance Algorithm for the Supplemental Demographic and Housing Characteristics File

William Sexton, Ashwin Machanavajjhala, David Pujol



# Goals

---

- What is PHSafe?
- Development workflow for deploying DP
  - How does PHSafe work?
  - When does PHSafe work well?
  - Why does PHSafe work?

# What is PHSafe?

---

## **Disclosure Avoidance and the Supplemental Demographic and Housing Characteristics File (S-DHC): How PHSafe Works**

---

*2020 Census Briefs*

By the Population Reference Bureau and  
the U.S. Census Bureau's 2020 Census Data Products and Dissemination Team

<https://www2.census.gov/library/publications/decennial/2020/census-briefs/c2020br-12.pdf>

## Tumult's Methodology for Deploying Differential Privacy

---

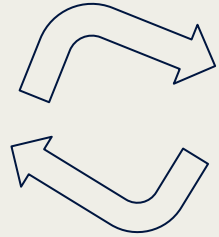
### Design



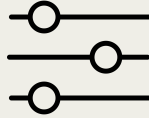
What are the tabular summaries to release?

What are the privacy and accuracy requirements?

What is the algorithmic strategy?



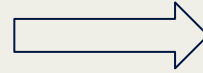
### Tune



What are the tunable parameters that affect privacy and accuracy?

Can we quantify the relationship between privacy and accuracy?

How do we choose the right parameters?



### Deploy



Is the algorithm implemented correctly? Is it provably private?

How do we communicate the privacy accuracy tradeoffs inherent in the implementation?

# Outline

---

- **Designing PHSafe**
- Tuning PHSafe
- Deploying PHSafe

# Design: What are the tabular summaries?

---

## PH1 Num

Average Household Size  
By Age

## PH1 Denom

Average Household Size  
By Age

## PH2

Household Type for the  
Population in  
Households

## PH3

Household Type by  
Relationship for the  
Population Under 18  
Years

## PH4

Population in Families  
by Age

## PH5 Num

Average Family Size by  
Age

## PH5 Denom

Average Family Size by  
Age

## PH6

Family Type and Age for  
Own Children Under 18  
Years

## PH7

Total Population in  
Occupied Housing Units  
by Tenure

## PH8 Num

Average Household Size  
of Occupied Housing  
Units by Tenure

## PH8 Denom

Average Household Size  
of Occupied Housing  
Units by Tenure

# Design: What are the privacy and accuracy requirements?

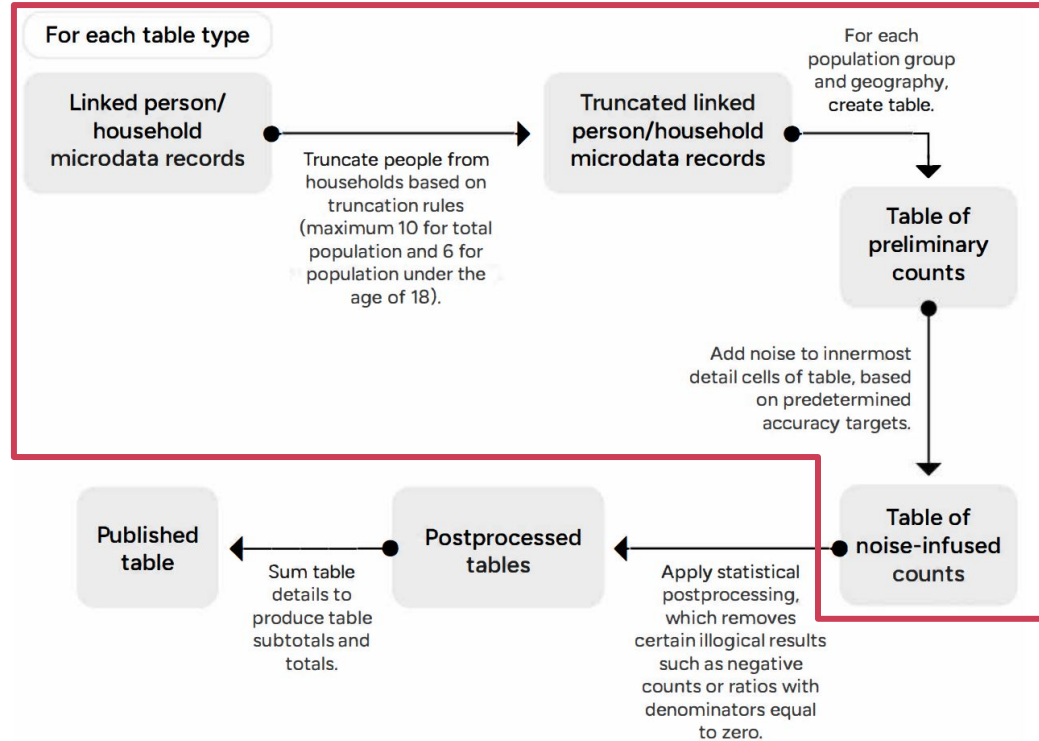
---

- **Privacy:** PHSafe must satisfy zero-concentrated differential privacy (zCDP).
  
- **Accuracy:** PHSafe's noise infusion must be tunable to achieve desired 90% margins of error (MOE).

# Design: What is the algorithmic strategy?

Figure 1.

## Steps in the PHSafe and Statistical Postprocessing Method



Source: U.S. Census Bureau.



# Joined Data

---

PersonID	HouseholdID	Relationship
Person 1	Household A	Householder
Person 2	Household A	Spouse
Person 3	Household A	Biological Child
Person 4	Household A	Biological Child
Person 5	Household A	Biological Child
Person 1	Household B	Householder
Person 2	Household B	Unmarried Partner

HouseholdID	Household Size	Household Type
Household A	5	Married Couple Family
Household B	2	Non Family
Household C	4	Single Parent Family

# Disclosure risks with Joined Data

---

PersonID	HouseholdID	Relationship
Person 1	Household A	Householder
Person 3	Household B	Biological Child
Person 3	Household A	Biological Child
Person 4	Household A	Biological Child
Person 5	Household A	Biological Child
Person 1	Household B	Householder
Person 2	Household B	Unmarried Partner

HouseholdID	Household Size	Household Type
Household A	4	Single Parent Family
Household B	3	Cohabiting Couple Family
Household C	4	Single Parent Family



# Disclosure risks with Joined Data

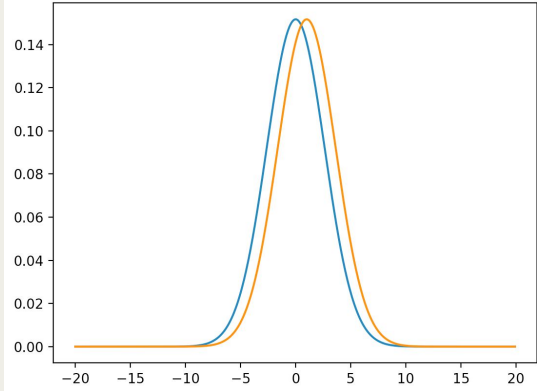
PersonID	HouseholdID	Relationship
Person 1	Household A	Householder
Person 3	Household B	Biological Child
Person 3	Household A	Biological Child
Person 4	Household A	Biological Child
Person 5	Household A	Biological Child
Person 1	Household B	Householder
Person 2	Household B	Unmarried Partner

HouseholdID	Household Size	Household Type
Household A	4	Single Parent Family
Household B	3	Cohabiting Couple Family
Household C	4	Single Parent Family

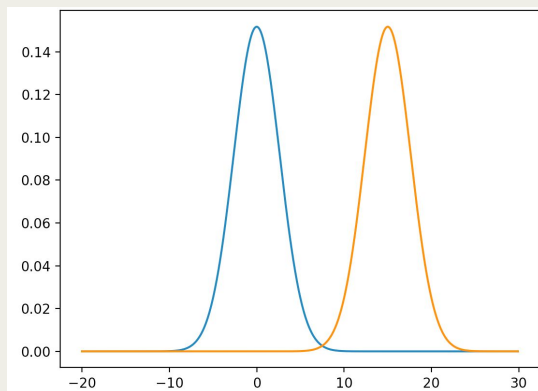
# Disclosure risks with Joined Data

---

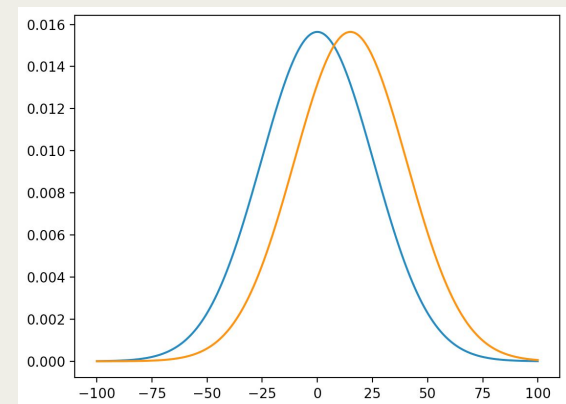
Low influence scenario.  
Max household size = 1  
MOE = 5, low disclosure risk



High influence scenario.  
Max household size = 15  
MOE = 5, high disclosure risk



High influence scenario.  
Max household size = 15  
MOE = 50, low disclosure risk



# Truncation

- Limits the number of people in households to not exceed a given threshold.
- Ignores out of universe
- Randomly selects in-universe records for removal as needed.

Table 2.

## Illustration of Truncation for Household Maximum of Six People Under the Age of 18

Initial household	Person number in the enumerated household	Age	In universe?	Action	Person number in the truncated household
Household A	1	51	Not in universe.	Exclude from universe.	Not in universe.
Household A	2	49	Not in universe.	Exclude from universe.	Not in universe.
Household A	3	17	In universe.	No change.	1
Household B	1	63	Not in universe.	Exclude from universe.	Not in universe.
Household B	2	40	Not in universe.	Exclude from universe.	Not in universe.
Household B	3	22	Not in universe.	Exclude from universe.	Not in universe.
Household B	4	2	In universe.	No change.	1
Household B	5	5	In universe.	No change.	2
Household B	6	1	In universe.	No change.	3
Household B	7	2	In universe.	Selected at random for removal.	Not included.
Household B	8	5	In universe.	Selected at random for removal.	Not included.
Household B	9	6	In universe.	No change.	4
Household B	10	6	In universe.	Selected at random for removal.	Not included.
Household B	11	9	In universe.	No change.	5
Household B	12	17	In universe.	No change.	6
Household C	1	26	Not in universe.	Exclude from universe.	Not in universe.
Household C	2	22	Not in universe.	Exclude from universe.	Not in universe.
Household C	3	24	Not in universe.	Exclude from universe.	Not in universe.
Household C	4	23	Not in universe.	Exclude from universe.	Not in universe.
Household C	5	21	Not in universe.	Exclude from universe.	Not in universe.
Household C	6	21	Not in universe.	Exclude from universe.	Not in universe.
Household C	7	19	Not in universe.	Exclude from universe.	Not in universe.
Household C	8	19	Not in universe.	Exclude from universe.	Not in universe.
Household C	9	19	Not in universe.	Exclude from universe.	Not in universe.
Household C	10	18	Not in universe.	Exclude from universe.	Not in universe.
Household C	11	17	In universe.	No change.	1
Household C	12	17	In universe.	No change.	2

Source: U.S. Census Bureau.

# Truncation

---

## PH1 Num

Average Household Size  
By Age

$\tau = 10$

## PH2

Household Type for the  
Population in  
Households

$\tau = 10$

## PH3

Household Type by  
Relationship for the  
Population Under 18  
Years

$\tau = 6$

## PH4

Population in Families  
by Age

$\tau = 10$

## PH5 Num

Average Family Size by  
Age

## PH6

Family Type and Age for  
Own Children Under 18  
Years

$\tau = 6$

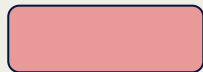
## PH7

Total Population in  
Occupied Housing Units  
by Tenure

$\tau = 10$

## PH8 Num

Average Household Size  
of Occupied Housing  
Units by Tenure



Not directly computed  
by PHSafe



Directly computed by  
PHSafe

# Noise Infusion

---

## PH2: Household Type for the Population in Households

*Universe: Population in households.*

Total:

In married couple household:

Opposite-sex married couple

Same-sex married couple

In cohabiting couple family:

Opposite-sex cohabiting couple

Same-sex cohabiting couple

Male householder, no spouse or partner present:

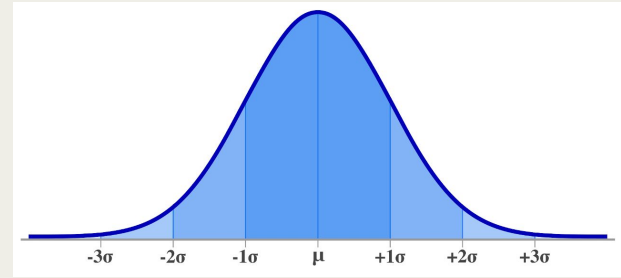
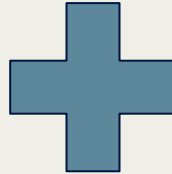
Living alone

Living with others

Female householder, no spouse or partner present:

Living alone

Living with others



# Noise infusion

The discrete Gaussian distribution  $\mathcal{N}_{\mathbb{Z}}(\sigma^2)$  centered at 0 is

$$\forall x \in \mathbb{Z}, \quad \Pr[X = x] = \frac{e^{-x^2/2\sigma^2}}{\sum_{y \in \mathbb{Z}} e^{-y^2/2\sigma^2}}.$$

$$\sigma^2 = (2\tau + 2)^2 / \rho$$

PH1_num	Total	Iteration H,I	Iterations A-G
Nation		??	
State			

PH2	Total
Nation	??
State	



# Outline

---

- Designing PHSafe
- **Tuning PHSafe**
- Deploying PHSafe

# Tuning: What are the tunable parameters that affect privacy and accuracy?

---

- Privacy-loss budget
- Truncation threshold
- 90% MOE
- Geography levels
- Race Iterations

# Tune: What is the relationship between privacy and accuracy?

---

$$\sigma^2 = (2\tau+2)^2 / \varrho$$

$$90\% \text{ MOE} = 1.645\sigma$$

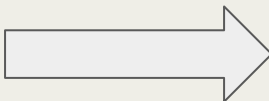
$$\varrho = 1.645^2(2\tau+2)^2 / \text{MOE}^2$$

$$\tau=10, \text{MOE}=200 \implies \varrho = 0.0327$$

# Tune: How do we choose the right parameters?

## 1. Specify Privacy Loss Budget Parameters

		Geography	
		Enabled	Total Epsilon
Geography	USA	TRUE	2.43
	Region	TRUE	0.54
	Division	FALSE	0.20
	State	TRUE	0.10
	County	FALSE	0.25
	Tract	TRUE	0.10
	Block Group	FALSE	0.20
	Block	TRUE	0.10
	Place	FALSE	0.54
	AIANNH	FALSE	0.10
Total epsilon budget for P30:			3.27



## 3. Set Truncation Thresholds

Truncation threshold:	25
Truncation algorithm:	Random truncation
Drop household above threshold	
Random truncation	

## 4. Choose Measurement



## Error for P30

Region type	Selected	Total epsilon	Level	Cell description	MOE*
USA	YES	0.00	0	Total:	145.20
USA	YES	2.19	1	In married couple household	72.60
USA	YES	0.00	2	Opposite-sex married couple	-
USA	YES	0.00	2	Same-sex married couple	-
USA	YES	2.19	1	In cohabiting couple household	72.60
USA	YES	0.00	2	Opposite-sex cohabiting couple	-
USA	YES	0.00	2	Same-sex cohabiting couple	-
USA	YES	2.19	1	Male householder, no spouse or partner present	72.60
USA	YES	0.00	2	Living alone	-
USA	YES	0.00	2	Living with others	-
USA	YES	2.19	1	Female householder, no spouse or partner present	72.60
USA	YES	0.00	2	Living alone	-
USA	YES	0.00	2	Living with others	-

# Tune: Production Parameters for PHSafe

Table	Truncation Threshold	Population Group Level	MOE Target	Unbounded Privacy Loss	Bounded Privacy Loss
PH1_num	10	(Nation, Unattributed)	500	0.002619	0.005238
		(Nation, A-G)	500	0.002619	0.005238
		(Nation, H-I)	500	0.002619	0.005238
		(State, Unattributed)	200	0.016371	0.032742
		(State, A-G)	68	0.141622	0.283244
		(State, H-I)	200	0.016371	0.032742
PH1_denom	NA	(Nation, Unattributed)	500	0.000022	0.000044
		(Nation, A-G)	500	0.000022	0.000044
		(Nation, H-I)	500	0.000022	0.000044
		(State, Unattributed)	200	0.000135	0.00027
		(State, A-G)	68	0.00117	0.00234
		(State, H-I)	200	0.000135	0.00027
PH2	10	(Nation, Unattributed)	500	0.002619	0.005238
		(State, Unattributed)	200	0.016371	0.032742
PH3	6	(Nation, Unattributed)	500	0.001061	0.002122
		(Nation, A-G)	500	0.001061	0.002122
		(Nation, H-I)	500	0.001061	0.002122
		(State, Unattributed)	200	0.006630	0.01326
		(State, A-G)	20	0.662976	1.325952
		(State, H-I)	200	0.006630	0.01326

# Outline

---

- Designing PHSafe
- Tuning PHSafe
- **Deploying PHSafe**

## NIST strongly recommends using well-tested DP libraries

18 NIST Special Publication  
19 NIST SP 800-226 ipd

20 **Guidelines for Evaluating Differential**  
21 **Privacy Guarantees**  
22

23 **Authors**

24 Joseph P. Near  
25 University of Vermont

26 David Darais  
27 Galois, Inc.

28 **Editors**

29 Naomi Lefkowitz  
30 Gary Howarth

31 Applied Cybersecurity Division, Information Technology Laboratory, NIST

32 This publication is available free of charge from:  
33 <https://doi.org/10.6028/NIST.SP.800-226.ipd>

34 December 2023



35 U.S. Department of Commerce  
36 Gina M. Raimondo, Secretary

37 National Institute of Standards and Technology  
38 Laurie E. Locascio, NIST Director and Under Secretary of Commerce for Standards and Technology

**Privacy Hazard** Avoid custom implementations of differentially private algorithms, and use well-tested libraries instead.

**Privacy Hazard** Implementing differential privacy mechanisms is tricky and requires considering side-channel vulnerabilities.

**Privacy Hazard** When bounding user contributions, additional noise must be added to ensure user-level privacy.

**Privacy Hazard** In differentially private histograms, the analyst must specify the histogram bins. Otherwise, the presence or absence of a bin may leak information that violates differential privacy.

```
session = Session.from_dataframe(  
    dataframe=private_data,  
    source_id="my_data",  
    RhoZCDPBudget(1.5)  
)  
  
query = (  
    QueryBuilder("my_data")  
    .filter("age < 18")  
    .groupby(states)  
    .count()  
)  
  
result = session.evaluate(  
    query,  
    RhoZCDPBudget(0.2)  
)  
  
print(session.remaining_privacy_budget())  
# prints RhoZCDPBudget(1.3)
```

# Tumult Analytics

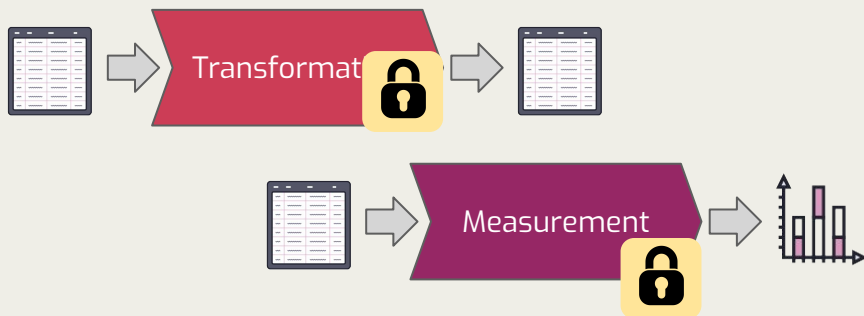
Intended for data scientists

- DP expertise *not* required
- Python interface similar to pandas/spark

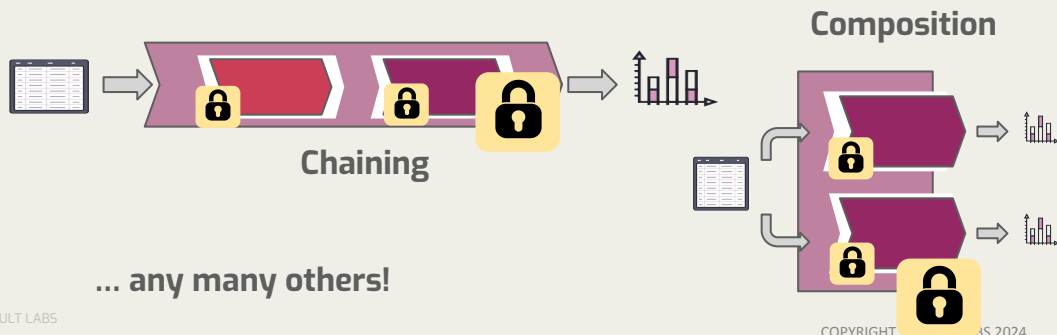


# Tumult Core

A collection of composable components: transformations and measurements.



Combinators create new components from existing ones.



... any many others!

Core enables creation of complex algorithms from building blocks

Everything carries an explicit, inspectable privacy guarantee 🔒

Every DP computation in core comes with a proof of privacy

# Conclusion

---

- What is PHSafe? S-DHC's privacy protection algorithm.
- Development workflow for deploying DP
  - How does PHSafe work?.....**Algorithm designed by privacy experts**
  - When does PHSafe work well?.....**Algorithm tuned by subjected-matter experts**
  - Why does PHSafe work?.....**Algorithm deployed on Tumult Analytics**